

A STUDY ON AGENT SCHEDULING SCENARIOS IN MULTI-AGENT SYSTEMS

¹CECILIA E. NUGRAHANI, ²LUCIANA ABEDNEGO

^{1,2}Department of Computer Science, Parahyangan Catholic University, Indonesia

E-mail: ¹cheni@unpar.ac.id, ²luciana@unpar.ac.id

ABSTRACT

A multi-agent system (MAS) is understood as a collection of intelligent agents that interact with each other and work together to achieve a goal. Since it consists of many agents, the communication, coordination, and scheduling among agents are important issues in MAS. This paper presents a study on the effect of agent scheduling on the performance of a MAS. The study is conducted on a small parameterized MAS, which is a Sudoku solver. Four agent scheduling scenarios have been developed and implemented. Some experiments have been conducted to measure the performance of each scenario. It is shown that the scheduling scenarios have effect on the system performance.

Keywords: *Multi-Agent Systems, Agent Scheduling Scenario, Sudoku, Sudoku Solver, Block World Problem*

1. INTRODUCTION

Multi-Agent Systems (MAS) has become one of popular paradigms for understanding and building complex systems, especially distributed systems [1, 2]. This paradigm is widely used to develop nowadays systems. It has been applied in various fields, e.g. in health and medical [3,4], traffic and transportation [5,6], etc.

A MAS is understood as a collection of intelligent agents that interact with each other and work together to achieve a goal. In this context, the agents are software or computer programs. Since it consists of many agents, the communication, coordination, and scheduling among agents are important issues in MAS.

This work focuses on an important issue of MAS which is scheduling. The objective of this research is to analyze the effect of scheduling scenario on the performance of a MAS. By knowing the effect of the agent scheduling scenarios, we can apply an appropriate or optimal scheduling scenario in order to get the best performance of a MAS.

Various reviews on MAS can be found in literature, ranging from the aspect of architecture, agent communication, agent scheduling, modeling, verification, performance, and application of MAS. In particular, there are many research related to performance evaluation of MAS, e.g. performance comparison of two information retrieval MAS: the one contains stationary agents only and the other

contains one mobile agent [7], performance comparison between two MAS for combinatorial auction and voting with different architecture and agent communication [8], comparative study of two different open-source MAS architectures [9], and comparison between centralized and decentralized scheduling approach of MAS [10]. Similar to [10], this work focuses on the effect of scheduling algorithm on the performance of MAS.

As case study we took MAS-based Sudoku solver [11,12]. A research related to MAS that also used Sudoku as the case study is found in [13]. However, the modelling of Sudoku in [13] is different from our model. We use BWP-based Sudoku Solver that, in our knowledge, has been never used before by other researchers.

We limited our work on a class of MAS which is parameterized MAS. This makes the difference between this work and the others. The underlying concept of parameterized MAS is parameterized systems proposed in [14]. More work related to parameterized systems can be found in [15,16,17]. We also limit our work to the interleaving systems which means that at every time there is maximum one active process.

The main contribution of this paper is to enrich the results of research related to MAS, particularly to the issues that affect the performance of MAS. In addition, this paper also shows how a simple case

study like Sudoku puzzle can be used to study complex systems.

The rest of this paper is structured as follows. Section 2 explains the concept of BWP and how to model Sudoku Solver as BWP. Section 3 presents our BWP-based Sudoku solver that we used for the case study. Section 4 and section 5 describes the scheduling scenarios and the experimental results, respectively. Conclusion and future work are given in Section 6.

2. MODELLING SUDOKU PUZZLES AS BWPS

A BWP consists of a set of blocks, a table, and two robots. The blocks are initially arranged in some vertical stacks. Each robot has its own task capability: the first robot is capable to take a box at a top of a stack and put it on the table, whereas the second robot is capable to take a box on a table and put it on a top of a stack. The problem is how to change the initial arrangement to a new different arrangement by using the two robots. Several approaches for modelling and solving BWP can be found in literature, for example in [18]. An illustration of a BWP is given in Figure 1.

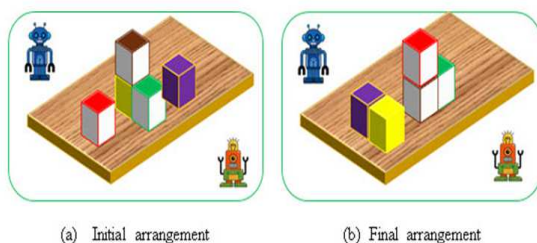
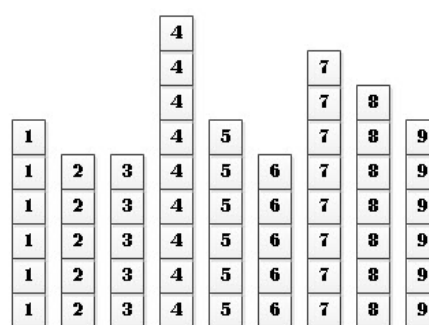
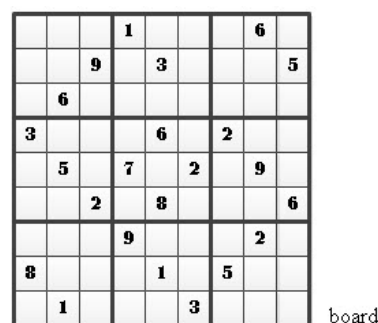


Figure 1. A Block World Problem.

BWP is frequently used in explaining the concept of Multi-Agent Systems. In particular, in [17] BWP is used as a case study for formal modelling and verification of parameterized MAS. A parameterized MAS is a MAS consisting a number of similar agents. The number of the agents is given as parameter of the system. It is assumed that the system is interleaving, that means there is only one agent works at a time.

Inspired by [17], we have proposed a novel approach for solving Sudoku puzzles, which is by modelling Sudoku puzzles as BWPs [11]. By modifying some settings of block world problem we have shown that Sudoku puzzles can be regarded as a variant of BWP. The modification is illustrated in Figure 2.



Piles of boxes outside the board

Figure 2. Modification of a BWP.

Three models for BWP based Sudoku solver have been defined in [11]. The difference among the models lies on the number and the task or the capability of the robot.

The first model uses two robots and is based on backtracking principle. This model is very similar to the original BWP. The first robot's task is to take a box and tries to put on a cell on the board which is valid for the box. Whereas the second robot's task is to take a box from a cell and put it back to the stack outside the board. The first robot gets the first turn, repeatedly does it task until all cells are filled with boxes or it is unable to find a box that can be placed on an empty cell. If the last condition holds, then the second robot will do its task by taking the last box put by the first robot from the board. The searching for a solution is then continued. Given a valid Sudoku puzzle, model 1 guarantees that a solution will be found.

The second and third models use nine robots and use fixed-point principle, instead of backtracking principle. The solution searching process is done by making iterations until a termination condition is reached. At each iteration, each robot i tries to find an appropriate cell or a valid position for a box with number i . If the searching succeeds, then it puts a

box with number i on that cell. After doing its job, the robot i will give the turn to the next robot. After the robot 9 does its job, it will be decided whether a new iteration should be made or not. If in the last iteration, all the robots cannot find appropriate cells, then the process is stopped. Differs from the first model, the second and the third model cannot guarantee to find a solution for a, even, valid puzzle.

Later, a new Sudoku Solver model has been proposed [12]. All four models have been successfully implemented and tested on 100 Sudoku puzzles. The experimental results show that the first model provides the best performance, followed by the fourth model. It is also reported that the combination of model 4 and model 1 gives improvement to the performance of the Solver.

In [12] all the models apply the same agent scheduling scenario. In this work, we will study the effect of agent scheduling on the performance of the Sudoku Solver. For that purpose, we define four scheduling scenarios. We apply each scenario on the fourth model. Experiment will be conducted to measure the performance of each scenario. We then compare the performance of each scenario with the original scenario.

3. BWP-BASED SUDOKU SOLVER

A Sudoku puzzle can be viewed as a BWP whose elements are a table, a board, a set of boxes and a set of robots [11,12]. The board comprises of 3×3 sub-blocks, each sub-block is a 3×3 cells, and is located on the table. The number of the boxes is 9×9 . Each box is labeled with a number within 1 to 9. For each label there are 9 boxes labeled with this number. The initial arrangement is the arrangement of the boxes so that there are some boxes are already put on the cells of the board and the rest of the boxes are outside the board. The boxes outside the board are organized in piles according to their numbers. The final arrangement is the arrangement of the boxes satisfying these conditions: all boxes are on the cells of the board, there are no boxes with the same label in the same row, the same column, and the same sub-block.

In this work, we used the fourth model proposed in [12]. Nine robots with the same capability are used by this model. Each robot is identified with a number from 1 to 9. Every robot is responsible to the stack of boxes according to its identifier. The task of the robots is to take a box from their corresponding stacks and put the box on a cell with

valid position of the board. A valid cell is defined as follows:

Definition 1 A robot i will call a cell at (x, y) a valid position if all the following conditions hold:

- 1) It is empty.
- 2) The row x does not contain any boxes with number i .
- 3) The column y does not contain any boxes with number i .
- 4) The sub-block where (x, y) is located does not contain any boxes with number i .
- 5) For every other row r in the same sub-block there is a box with number i or all cells in row r in the same sub-block with the cell (x, y) are not empty or the cell at the position (r, y) is not empty.
- 6) For every other column c in the same sub-block there is a box with number i or or all cells in column c in the same sub-block with the cell (x, y) are not empty or the cell at the position (x, c) is not empty.

For example, Figure 3 illustrates a valid position for robot 5.

	column								
	1	2	3	4	5	6	7	8	9
1		2			5			1	4
2	5			8		9			2
3			6				9		
4		5						6	
5	6								3
6		9							4
7			8	5			1	3	
8	3			9	2	4			6
9		6	5		8	7		2	

Figure 3: A valid position for robot 5.

To solve a puzzle, the solution searching process is done iteratively. At each iteration, the robots work one by one, in ascending order, starting from robot 1. Every time there is only one robot that works. In our implementation, a special module, called scheduler, is used to control this mechanism.

4. SCHEDULING SCENARIOS

In previous section we have explained that the solution searching process is done iteratively. At each iteration, each robot is given an equal opportunity to carry out its task. The ordering of

agent is always the same, from 1 to 9. The searching process is stopped whenever at an iteration all robots fail to do their tasks.

By analyzing the fourth model, we can conclude that there are interdependencies among the robots in doing their tasks. Let's consider the Sudoku puzzle in Figure 4 and focus on the upper middle sub-lock. Now assume that at an iteration, the robot 3 gets its turn before the robot 8. At this situation, the robot 3 cannot do its task successfully. There are two possible cells that can be taken, which are (1,4) and (3,4). However, the robot 3 has no capability to choose one of them due to the definition of valid position. The situation will be different if the robot 3 gets its turn after robot 8. Since robot 8 manages to put a box on cell on (1,4), therefore robot 3 can put a box on cell (3,4).

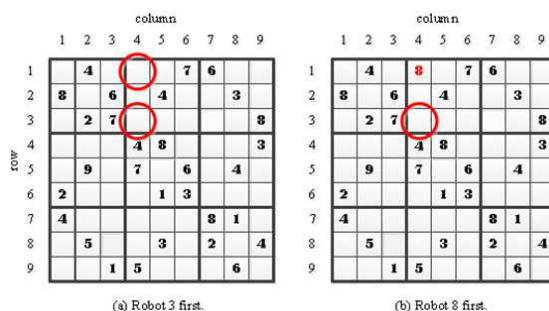


Figure 4: Two robot ordering scenarios

Based on the analysis, we draw a hypothesis that the agent ordering may bring effects on the performance of the Solver.

Since our focus is on the ordering of the robots, we define four scheduling scenarios that use random ordering principle. The first scenario (S1) and the second scenario (S2) are very similar to the original scenario (OS). Each scenario is described as follows:

- First scenario – S1

This scenario is very similar to OS, except before the *first iteration*, the scheduler generates an arbitrary permutation of a set {1, ..., 9}. This permutation is then used as the ordering of agents. The algorithm is given in Figure 5.

```
ordering <- permutation(1,9)
repeat
  res <- false
  for (i in 1..9) do
    res <- res or action(ordering[i])
  endfor
until not res
```

Figure 5: S1 Algorithm.

- Second scenario – S2

This scenario is very similar to OS, except before *every iteration*, the scheduler generate an arbitrary permutation of a set {1, ..., 9}. This permutation is then used as the ordering of agents. The algorithm is given in Figure 6.

```
repeat
  ordering <- permutation(1,9)
  res <- false
  for (i in 1..9) do
    res <- res or action(ordering[i])
  endfor
until not res
```

Figure 6: S2 Algorithm.

For the third (S3) and the fourth (S4) scenarios, at any iteration the scheduler picks a robot randomly. The searching process will be stopped whenever a stopping condition is reached. The difference between the both scenarios is on the stopping condition.

- Third scenario – S3

The stopping condition for S3 is defined as a condition when after a number of consecutive iteration there is no robot that can do its task successfully. As consequence, the scheduler has to record the number of failures. This number is reset whenever a successfully do its task. The algorithm is given in Figure 7.

```
counter <- 0
while (counter < max) do
  i <- pick_one_robot_randomly()
  if (action(i)) then
    counter <- 0
  else
    counter <- counter + 1
  endif
endwhile
```

Figure 7: S3 Algorithm.

- Fourth scenario – S4

S4 is an improvement of S3. The improvement is done by adding a process after the stopping condition for S3 is reached. Before stopping the process, scheduler will ask every robot to do its task, from robot 1 to robot 9. If there is a robot doing its task successfully, the searching process is continued. The algorithm is given in Figure 8

5. EXPERIMENTAL RESULTS

We have implemented all scenarios and conducted some experiments to measure the performance of each scenario. Each scenario is tested on 100 Sudoku puzzles with different level of difficulty. The puzzles are the same puzzles used

in [12]. Since each scenario contains a randomness factor, for each scenario we run the Solver 9 times for each puzzle. For S3 and S4, we set *max* to 20.

```

stop <- false
while not stop do
  counter <- 0
  while (counter < max) do
    i <- pick_one_robot_randomly()
    if (action(i)) then
      counter <- 0
    else
      counter <- counter + 1
    endif
  endwhile

  if (counter = max) then
    i <- 1
    succeed <- false
    resA <- false
    while (i <= 9 && not resA) do
      resA <- action(i)
      i++
    endwhile
    stop = not resA
  endif
endwhile
    
```

Figure 8: S4 Algorithm.

Our first experiment is to measure the average time needed by the Solver with a particular scenario in solving a Sudoku puzzle. From 100 puzzles, each scenario is only capable of solving 44 puzzles. This is the same number and the same puzzles that can be solved by OS. Without considering the puzzles that cannot be solved, the average time for solving a puzzle are shown in Table 1. We can see that S1 has the minimum average time, followed by S2, OS, S3, and the last is S4.

Table 1. Average Time for Solving a Puzzle

No	OS	S1	S2	S3	S4
1	8656	9920	9743	14994	15460
2	8469	9087	7831	12468	14058
3	13657	12392	11644	16949	17774
4	8500	8573	7465	12221	13951
5	10125	8964	8702	13572	14407
6	11203	9738	9724	13337	15593
7	8250	7767	8611	11234	14551
8	11109	10210	10137	15210	15048
9	12406	10925	10493	16435	15661
10	11266	8936	10853	14830	14084

Table 1. Average Time for Solving a Puzzle (cont.)

No	OS	S1	S2	S3	S4
11	8578	8071	11248	12596	14259
12	12422	11818	11542	15102	18108
13	9984	8052	11841	14753	14247
14	9906	9196	12267	13813	14979
15	8750	9161	11965	13106	14634
16	9860	9561	7823	14112	15020
17	12453	10182	8514	15049	15996
18	9890	9443	8925	12493	13988
19	9797	9238	9345	13493	13616
20	12063	10570	9821	14717	15734
21	16218	13918	16934	18372	19457
22	20093	15606	19307	15540	21804
23	15391	15017	17423	17907	19278
24	26875	14455	19866	24063	27181
25	18421	12856	17151	23121	20797
26	19938	15055	19077	27486	17774
27	12031	10818	13106	18422	17742
28	18781	13277	14967	19716	17160
29	17344	14002	14920	22904	21692
30	18625	15939	18339	25142	23612
31	17813	13398	19403	25781	24819
32	21282	17644	20047	25894	21761
33	16187	12779	16488	27276	22672
34	15657	13471	14312	21136	20963
35	24860	19885	21119	24141	24272
36	11844	9975	12774	17541	16421
37	50578	13272	15984	23656	19248
38	13703	11147	12780	19065	17249
39	13578	11894	13477	17170	19400
40	15579	17217	17001	23245	25805
41	15016	13858	14769	16941	17817
42	12328	11325	12170	15386	15987
43	16750	22077	21932	21994	26351
44	11937	10890	11295	13369	16121
Average	14561	11813	13181	17457	17961

Table 2 shows how many times a scenario has the minimum average time. It can be seen that, except S4, three other scenarios, S1, S2, and S3, are able to beat OS, at least once. From this result we can say that agent ordering scenarios may bring effects to the performance of the solver.

Table 2. Minimum Average Time

Scenario	min. average time (times)
OS	4
S1	27
S2	12
S3	1
S4	0

The algorithm of S4 is more complex than the other scenarios, as predicted, S4 provides the worst performance in this experiment. For S3, from 9 attempts for solving a puzzle, it not always the case that all attempts succeed. The worst case is from 9 attempts, there are only two attempts that succeed.

Furthermore, we measure the performance based on the number of empty cells that can be filled by the Solver using each scenario. The results are presented in Table 3. Table 4 presents the percentage of the empty cells that can be filled by each scenario. It can be seen that except S3, every scenario has the same performance.

If we pay more attention to the number of puzzles that can be solved by each scenario and also the percentage of filled cells, the new scenarios' performances are not better than OS. In other words, the new scenarios don't bring any significant improvement to OS. Moreover, S3 provide a worse performance than OS.

Table 3. The Number of Filled Empty Cells

No	Total empty cells	OS	S1	S2	S3	S4
1	52	24	24	24	22.2	24
2	49	31	31	31	30.7	31
3	51	12	12	12	11.6	12
4	49	18	18	18	15.8	18
5	51	8	8	8	7.78	8
6	51	13	13	13	10.7	13
7	53	9	9	9	8.78	9
8	49	21	21	21	20.3	21
9	54	9	9	9	8.22	9
10	53	10	10	10	7.89	10
11	55	2	2	2	1.89	2
12	53	4	4	4	3.78	4
13	53	7	7	7	6.67	7
14	55	11	11	11	10.6	11
15	51	11	11	11	10	11

Table 3. The Number of Filled Empty Cells (Cont.)

No	Total empty cells	OS	S1	S2	S3	S4
16	51	8	8	8	7.56	8
17	55	8	8	8	7.89	8
18	54	9	9	9	9	9
19	53	9	9	9	7.44	9
20	55	14	14	14	11.7	14
21	53	7	7	7	7	7
22	57	2	2	2	2	2
23	57	2	2	2	1.78	2
24	57	2	2	2	2	2
25	53	8	8	8	8	8
26	57	1	1	1	1	1
27	53	25	25	25	23.2	25
28	57	1	1	1	1	1
29	57	2	2	2	1.78	2
30	55	2	2	2	1.89	2
31	58	0	0	0	0	0
32	57	0	0	0	0	0
33	57	0	0	0	0	0
34	57	4	4	4	4	4
35	57	2	2	2	1.33	2
36	58	7	7	7	6.67	7
37	57	2	2	2	1.89	2
38	53	9	9	9	8.89	9
39	57	1	1	1	1	1
40	57	3	3	3	2.11	3
41	53	10	10	10	8.89	10
42	53	10	10	10	8.78	10
43	60	1	1	1	0.89	1
44	57	5	5	5	5	5
45	55	3	3	3	2.78	3
46	57	1	1	1	0.78	1
47	53	17	17	17	13.7	17
48	57	0	0	0	0	0
49	53	3	3	3	2.78	3
50	61	2	2	2	1.89	2
51	57	0	0	0	0	0
52	57	1	1	1	1	1
53	57	1	1	1	1	1
54	57	1	1	1	0.89	1
55	58	6	6	6	5.67	6

Table 4. Percentage Filled Cells

Scenario	Filled cells (%)
OS	0.127
S1	0.127
S2	0.127
S3	0.117
S4	0.127

6. CONCLUSIONS

We have studied the effects of agent scheduling scenarios on the performance of MAS. In particular, we take a Sudoku solver as a case study. We have developed and implemented four agent scheduling scenarios, which S1, S2, S3, and S4. Each scenario uses a random ordering. From the experimental result, it can be shown that S1 provide the best performance in the aspect of time. Whereas in the aspect of the number of puzzles that can be solved by each scenario and also the percentage of filled empty cells, the new scenarios don't bring any significant improvement.

The algorithm applied by the solver is based on simple heuristics used in solving Sudoku puzzles manually. From the experimental result, we can draw the conclusion that the algorithm applied cannot be used to solve puzzles with high level difficulty. Therefore, our next plan is to find better algorithms for solving Sudoku puzzles.

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